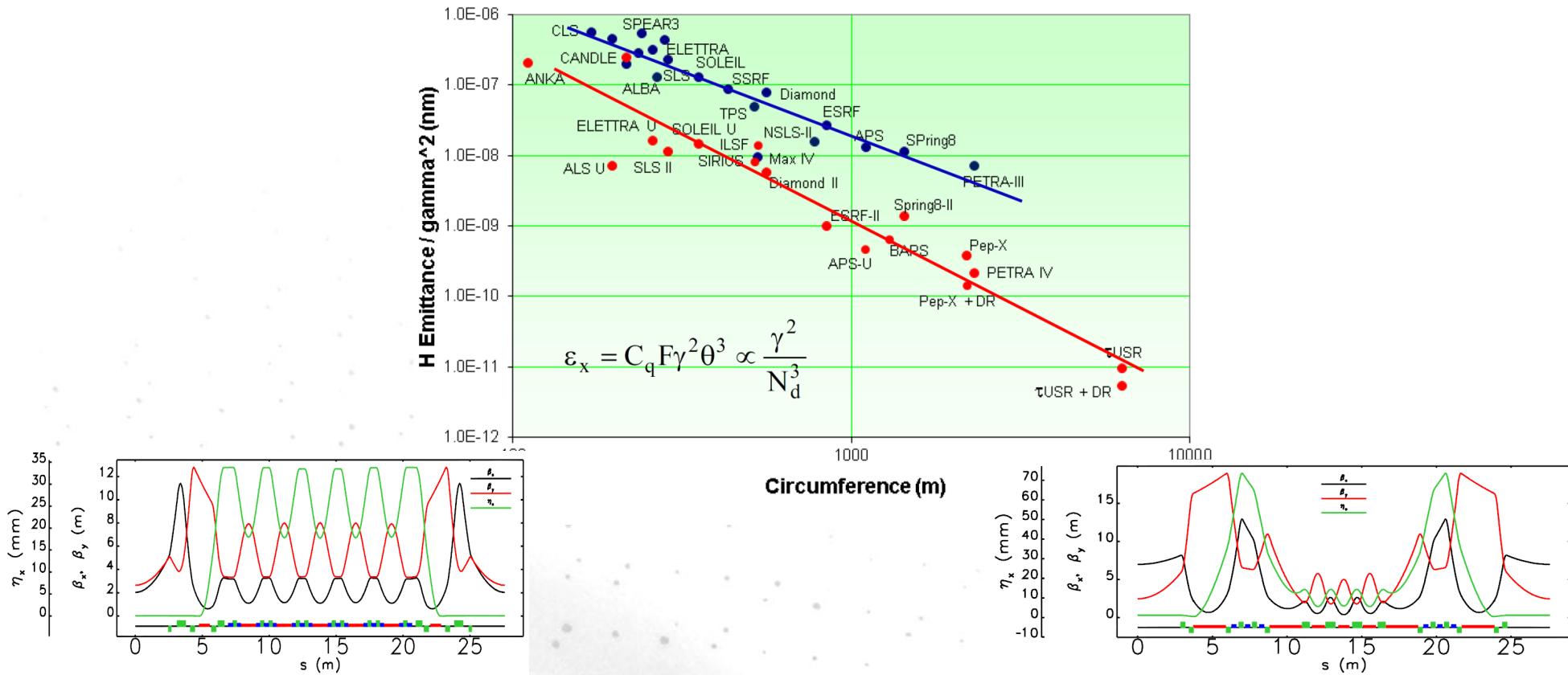


Review of Lattice Options for High-Brightness Light Sources

Laurent S. Nadolski
Accelerator Coordinator
Synchrotron SOLEIL

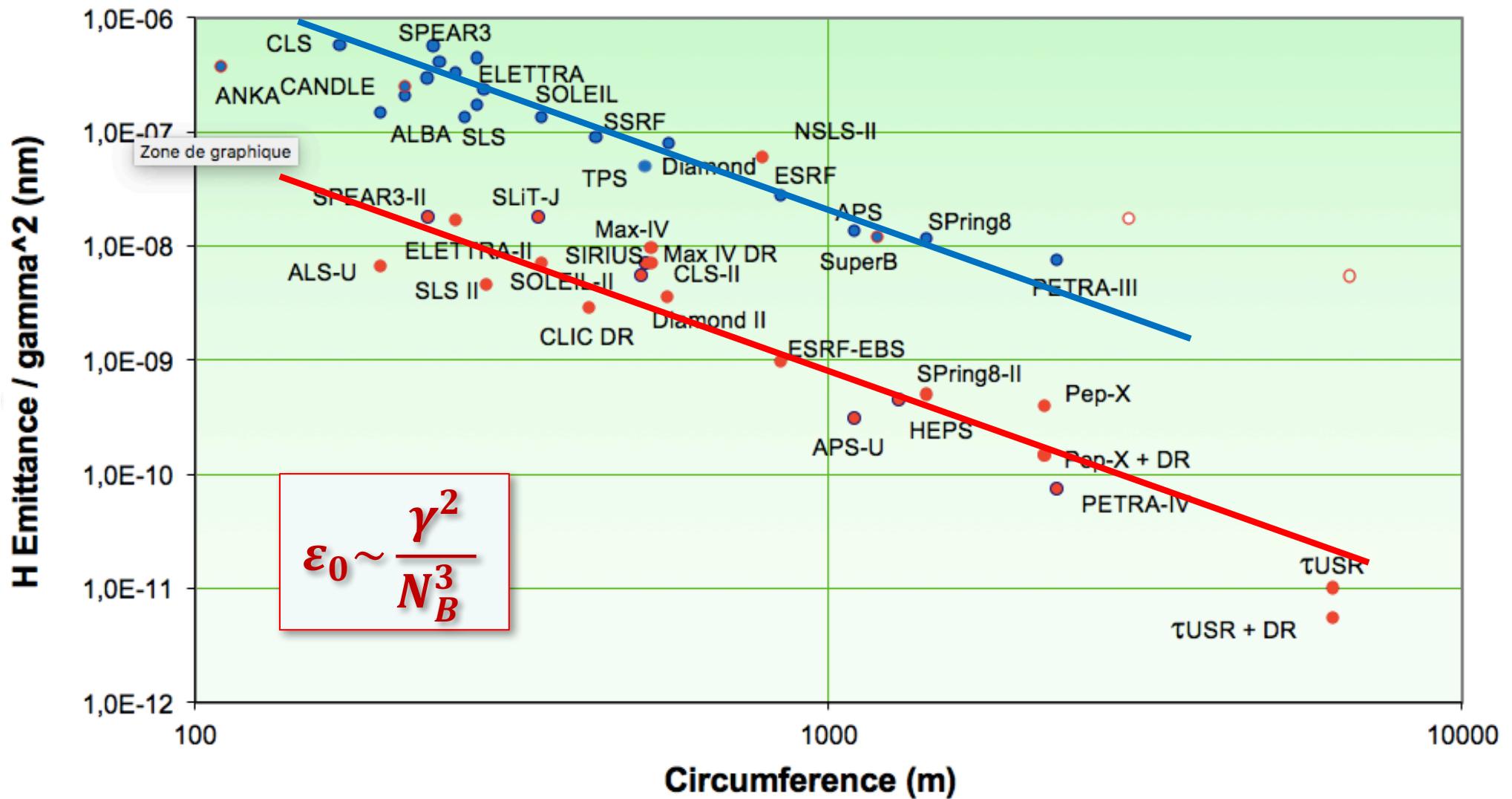


Contents

- High brilliance/low H-emittance
- Lattice design criteria
- Lattice review
- Summary and Conclusion



Roadmap to diffraction Limited Light sources (DLSR) High Brilliance Light sources (HBLS)



Adapted from R. Bartolini's plot

High brilliance achieved through MBA lattice

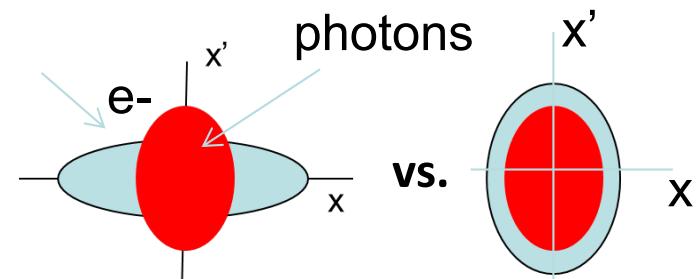
$$B_n(\lambda) = \frac{F_n(\lambda)}{4\pi^2(\varepsilon_x \oplus \lambda_n / 4\pi)(\varepsilon_z \oplus \lambda_n / 4\pi)}$$

$F_n(\lambda)$: Photon flux [photons/s/0.1% b.w.]

$\varepsilon_x, \varepsilon_z$: Transverse electron emittance

λ : Photon wavelength

($\lambda/4\pi$: diffraction limited photon emittance)



electron-photon ellipse adaptation

$$\begin{aligned} \varepsilon_0 [\text{nm rad}] &= 1470 E [\text{GeV}]^2 \frac{I_5}{J_x I_2}, \quad J_x = 1 - \frac{I_4}{I_2} \xrightarrow{\text{TME}} \text{MBA} \\ &= \frac{0.0078}{J_x} E [\text{GeV}]^2 \Phi [^\circ]^3 \frac{F(\beta_x, \eta)_\rho}{12\sqrt{15}}, \quad \Phi [^\circ]^3 \propto \frac{1}{N_b^3} \end{aligned}$$

Gradient Dipoles

$$I_2 = \oint \frac{ds}{\rho^2} \quad I_4 = \oint \frac{\eta}{\rho} \left(\frac{1}{\rho^2} + 2b_2 \right) ds \quad I_5 = \oint \frac{\mathcal{H}}{|\rho^3|} ds \quad \mathcal{H} = \gamma_x \eta^2 + 2\alpha_x \eta \eta' + \beta_x \eta^2$$

TME: brute-force approach $I_5/I_2 \rightarrow 0$ easily leads to overstrained optics, chromaticity wall

MBA: many weak dipoles, distributed chromaticity correction \rightarrow allows relaxing optics

Gradient dipoles: reduce emittance, allow for more compact optics \rightarrow improves MBA

TME Theoretical Minimum Emittance

Exploring the emittance formula

$$b = 1/\rho = B/(p/e)$$

Optic optimization leads to MBA

$$\varepsilon_0 \sim \frac{\gamma^2}{N_B^3}$$

horizontal focus in each dipole
many small dipoles

Longitudinal Gradient Bend
LGB

$$H = (\eta_x^2 + (\alpha\eta_x + \beta\eta'_x)^2)/\beta$$

$$I_5 = \int |b|^3 H ds$$

$$\varepsilon_{xo} [\text{m}\cdot\text{rad}] = \tilde{C}_q \gamma^2 \frac{I_5}{I_2 - I_4}$$

gradient bends

$$I_4 = \int b\eta(b^2 + 2k) ds$$

for vertical focusing ($bk < 0$)

TGB: transverse Gradient Bend



Radiated power

$$I_2 = \int b^2 ds$$

$$\Delta E [\text{keV}] = \tilde{C}_\gamma \gamma^4 I_2$$

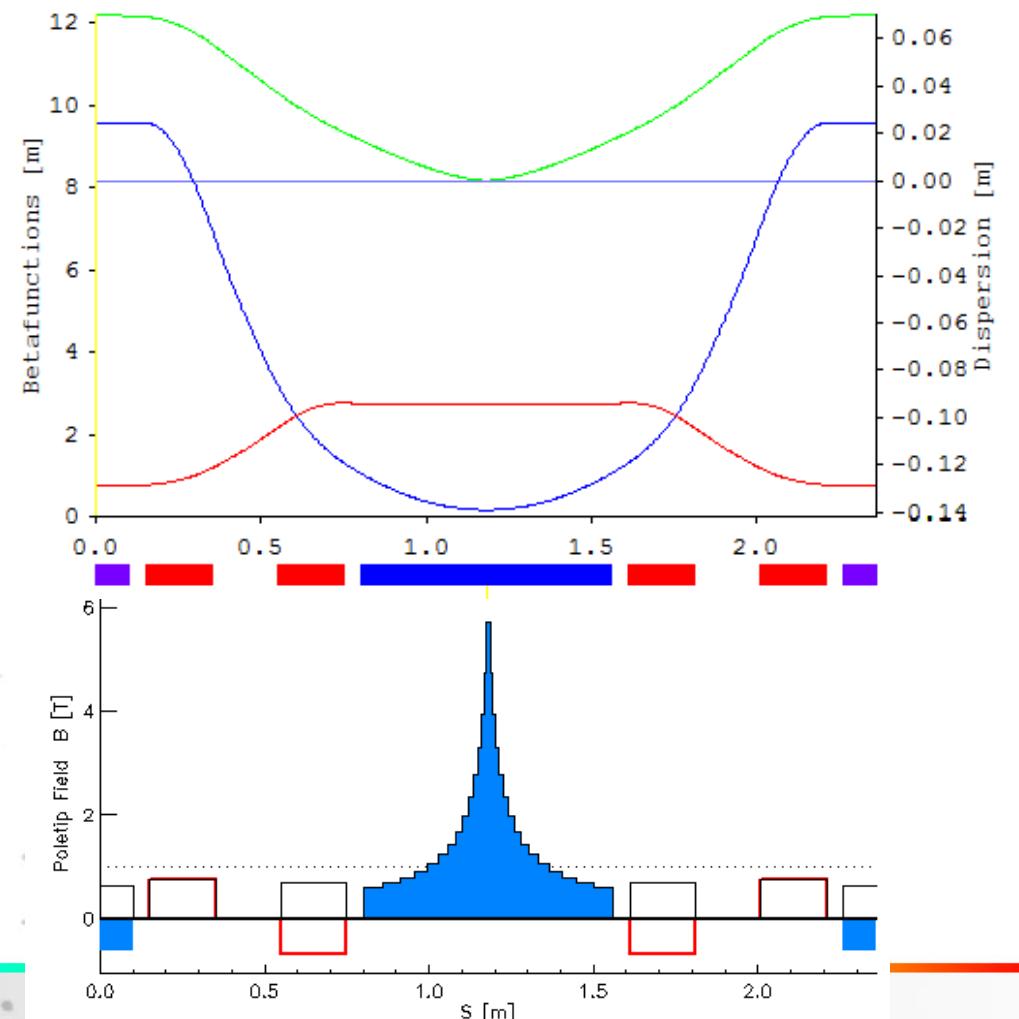
Damping wiggler

$$\tilde{C}_q = 3.83 \cdot 10^{-13} \text{ m} \quad \tilde{C}_\gamma = 9.60 \cdot 10^{-13} \text{ keV}$$

Ingredient: Longitudinal gradient bends

$$I_5 = \int |b|^3 H \, ds \quad b(s) = B(s)/(p/e)$$

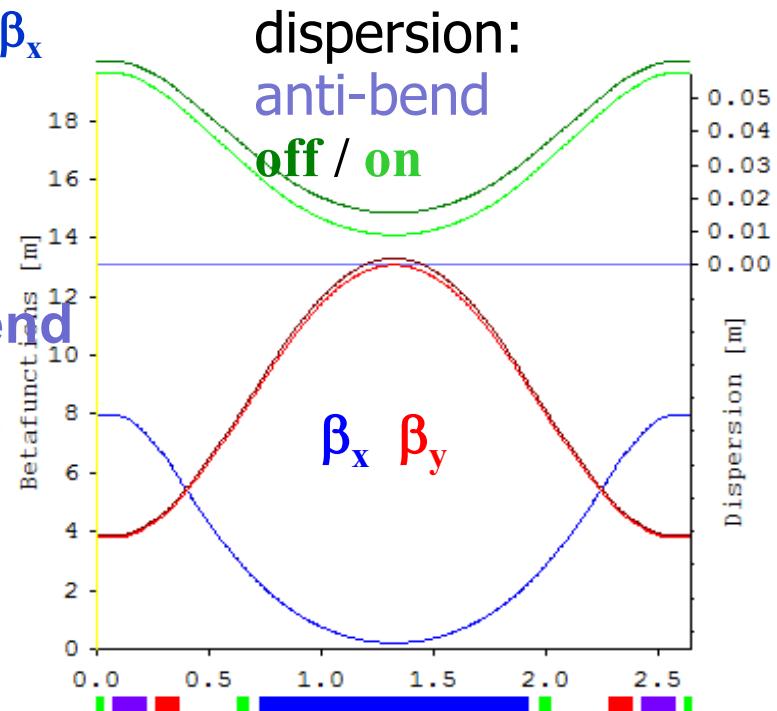
- **Longitudinal field variation**
 $b(s)$ to compensate $\mathcal{H}(s)$ variation
- Beam dynamics in bending magnet
 - Curvature is source of dispersion
 - Horizontal optics \sim like drift space
 - Assumptions: no transverse gradient ($k = 0$); rectangular geometry



Ingredient to lower the emittance: anti-bend

Courtesy of A.Streun

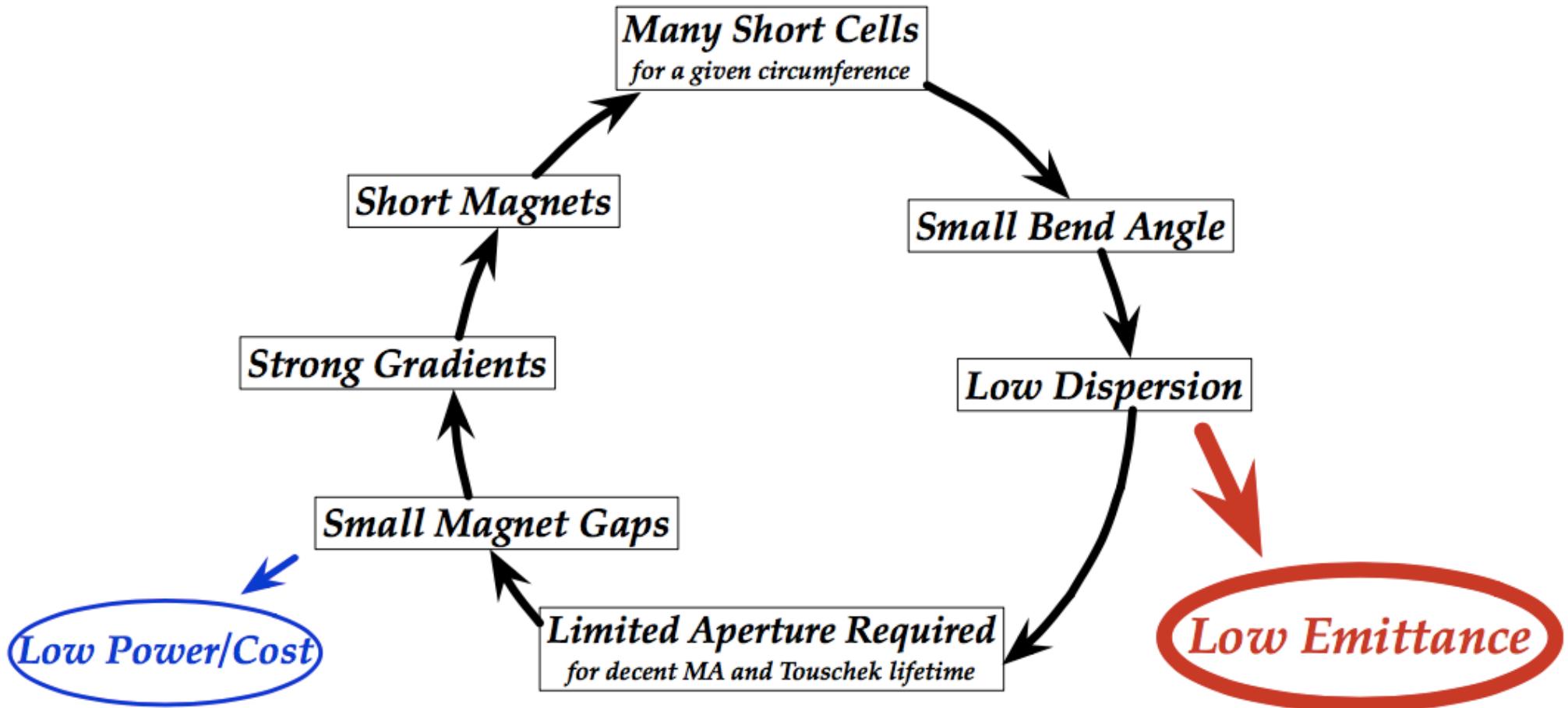
- **General problem of dispersion matching:**
 - dispersion production in dipoles → “defocusing”: $\eta' > 0$
- **Quadrupoles in conventional cell:**
 - dispersion is horizontal trajectory: quads treat η' and β_x in same way.
 - **over-focusing of horizontal** beta function β_x
 - **insufficient focusing** of dispersion η'
 - striking example: the TME cell
- disentangle η' and β_x !
- use negative dipole: **anti-bend/reverse bend**
 - kick $\Delta\eta' = \psi$, angle $\psi < 0$
 - out of phase with main dipole
 - negligible effect on β_x, β_y
- **Side effects on emittance:**
 - main dipole angle increase by $2|\psi|$
 - anti-bend located at large \mathcal{H}
 - in total, still lower emittance



TME: $F = 3.4, \varepsilon = 990 \text{ pm}$
LGAB: $F = 0.69, \varepsilon = 200 \text{ pm}$

The Multibend Achromat Cycle

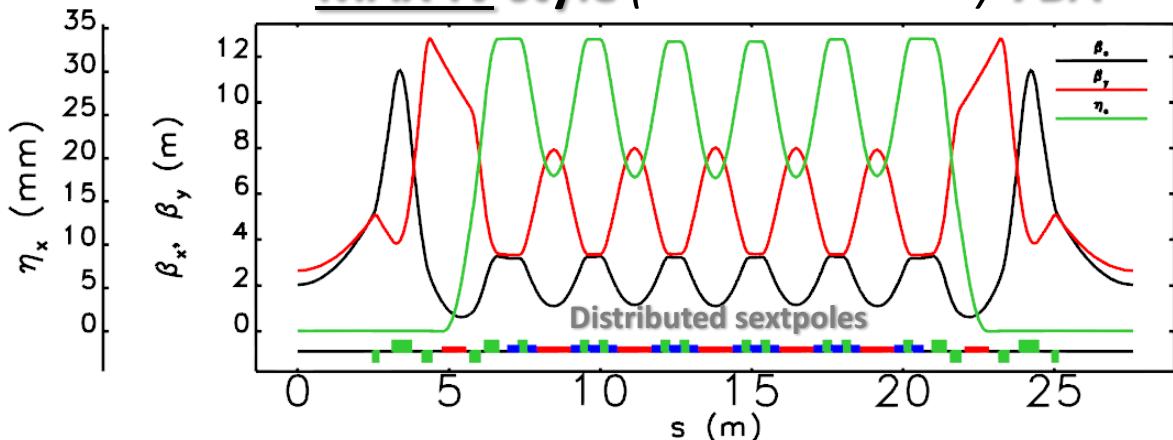
(courtesy A. Streun, PSI)



Deciding on the “M” part of the MBA.

$$\varepsilon_0 \sim \frac{\gamma^2}{N_B^3}$$

MAX-IV style (or ‘traditional’) 7BA*



SIRIUS MAX-IV

ELETTRA-II* SLS-II**

ALS-U*** CLS-II

SLiT-J

ESRF-EBS HEPS

PEPX APS-U*

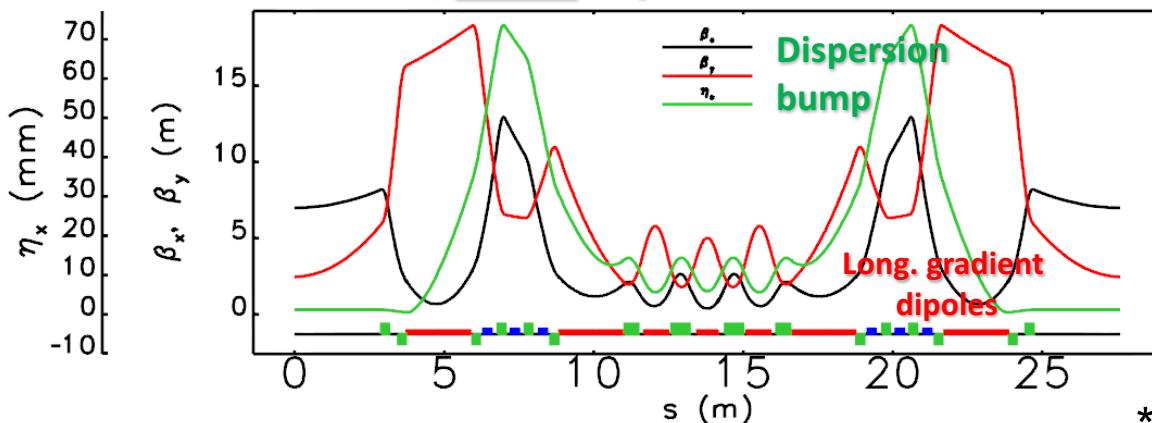
SPRing8-II PETRA-IV

DIAMOND-II***

SOLEIL-II***

* variation

ESRF/APSu style (or ‘hybrid’) 7BA*



Constraints to design a lattice Compromise-trade-off (1)

Budget

- Type of Machine: Green field lattice/Upgrade lattice
- Top-up (stability, reliability, lifetime/losses, MTBF, etc.),
- Requirement for Dipole-based beam lines
- Size of the ring/cell (compact/very large, ID lengths)
 - Large ring / hybrid lattice
- Number/Addition of straight sections/beamlines
- Compact lattice (tapers, flanges, bellows, RF-cavities, BPMs, etc.)
- Exotic magnets (LGB, Quad-dipole, combined magnets, all integrated magnets, Permanent magnet, Anti (reverse) bend)

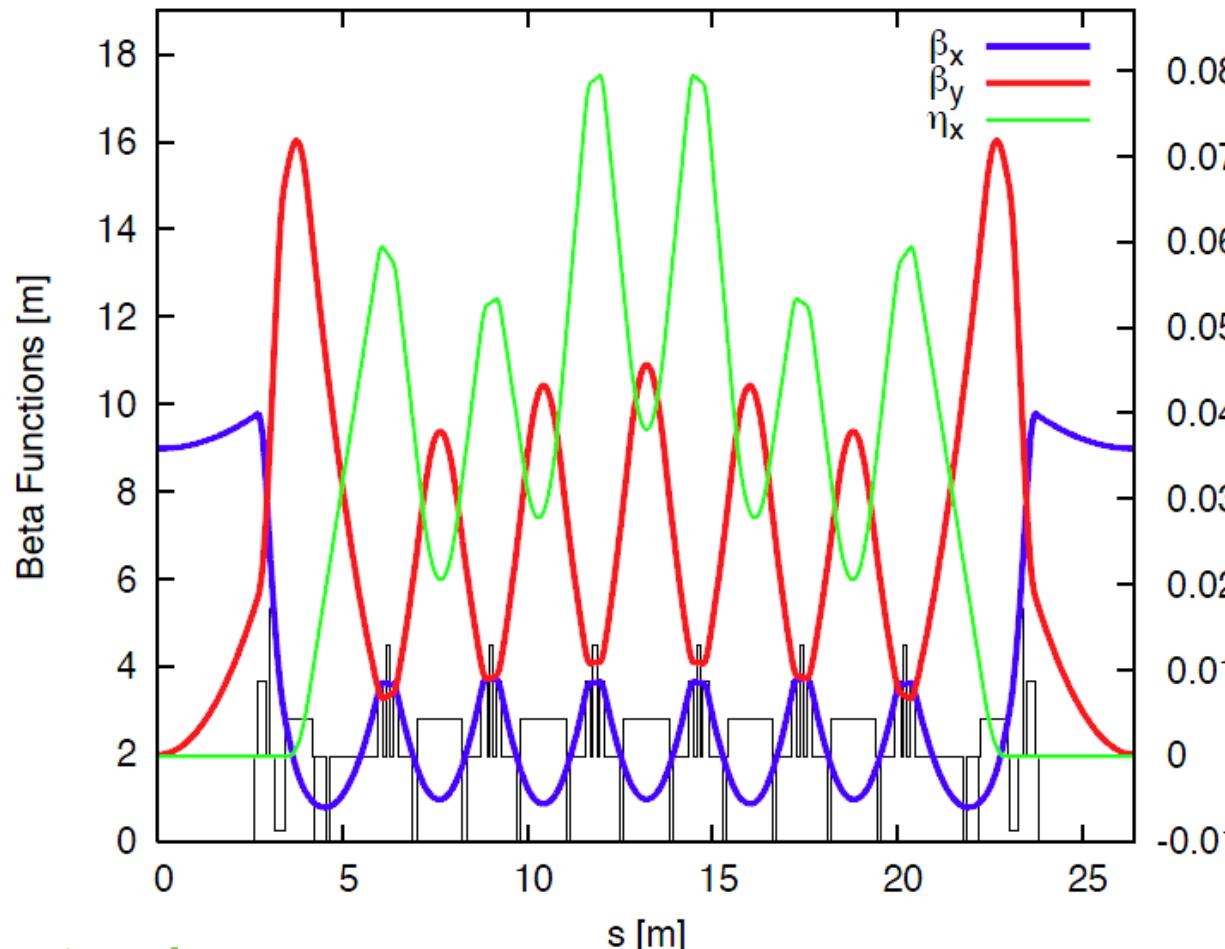
Constraints to select a lattice Compromise-trade-off (2)

- Injection scheme (off-axis/on axis/swap out, etc.)
- Technology limitations (quad/sextupole strength, space, etc.)
- Collective effect (IBS, Lifetime Time, ...)
- Lattice flexibility/tuneability
- Easy of operation (sensitivity to errors, IDs, etc.) /maintainability (MTTR)
- Maximum current / working chromaticities / filling-pattern

LATTICE REVIEW

**MAX-IV: 7BA, 3 GeV, 330 pm.rad, N=20,
528 m, 500 mA**

First DLSR MBA-based machine in operation



TME-cell + matching cells

Integrated solution

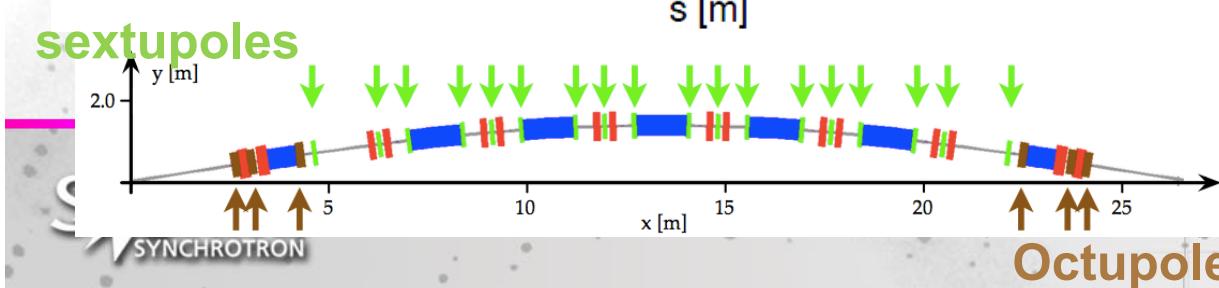
Compact design

Short straight sections

Off-axis injection, PMK*

No dipole source (low field gradient dipole)

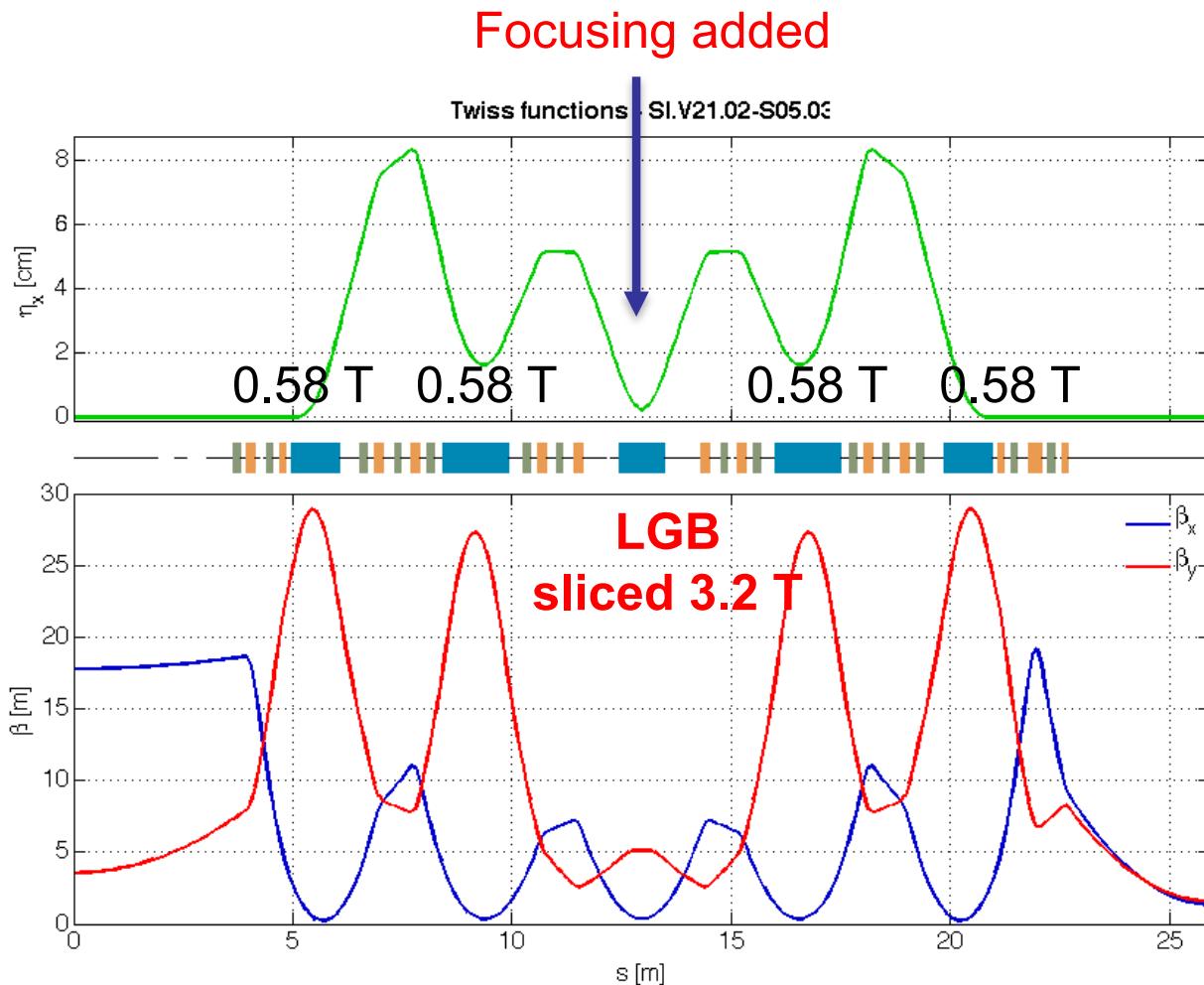
~Zero dispersion in SS



*PMK Pulsed Multipole Magnet

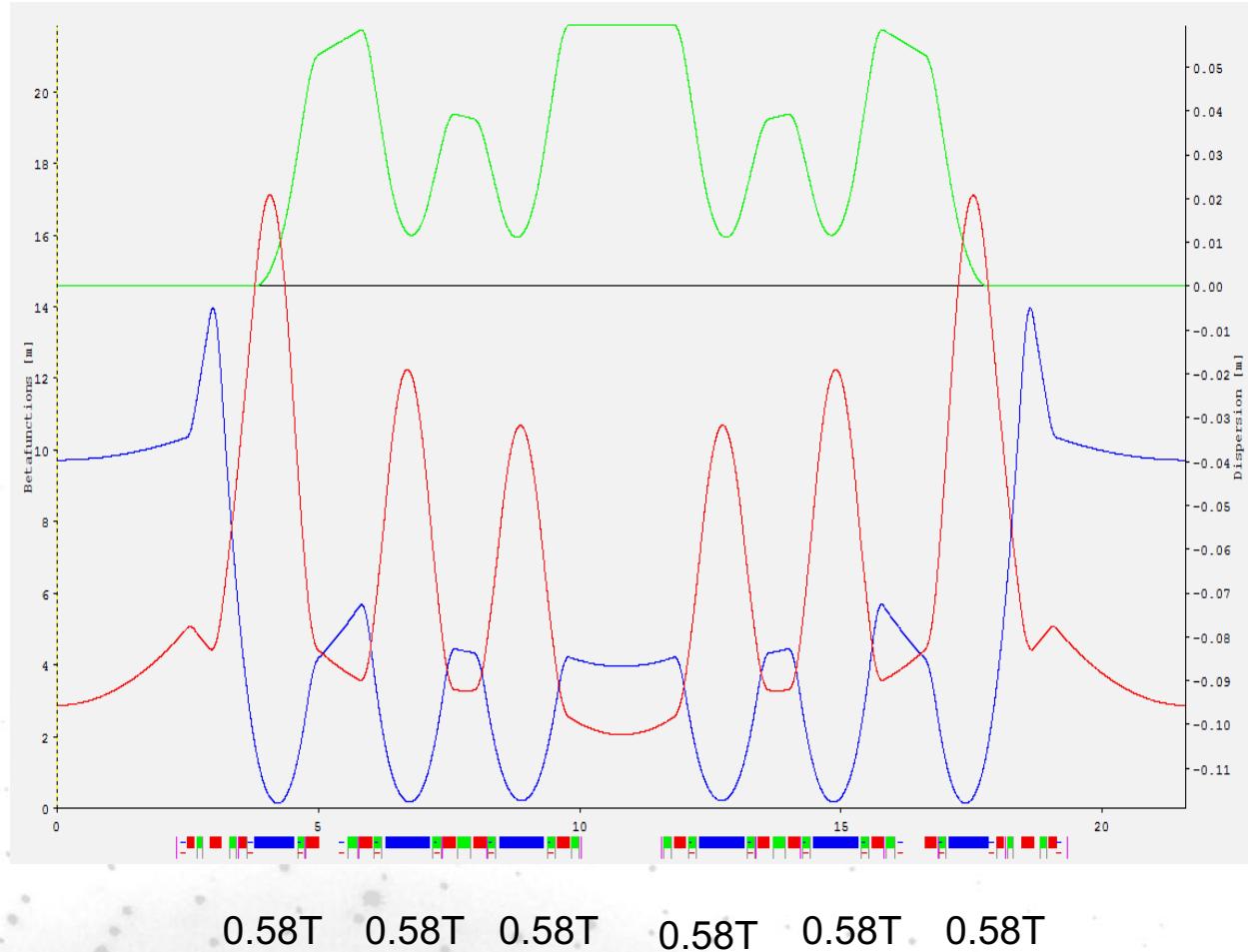


SIRIUS: 5BA, 3 GeV, 240 (150) pm.rad, N=20, 518 m, 500 mA



- 5-fold symmetric optics with **15 low and 5 high β sections.**
- Achromatic cells.
- At low β sections
 - $\beta_x \approx \beta_y \approx 1.5$ m
 - Optimized electron and photon beam phase-space matching for undulators.
- At **superbend (PM)**
 - Strong focusing of dispersion and β_x functions
 - Beam size: $9.5 \times 3.5 \mu\text{m}^2$
- **Off-Axis injection**
- pulsed multipole magnet

ELETTRA-II: Special* S6BA, 2 GeV, 250 pm.rad, N=12, 259.2 m



Dipole source

Easy to use

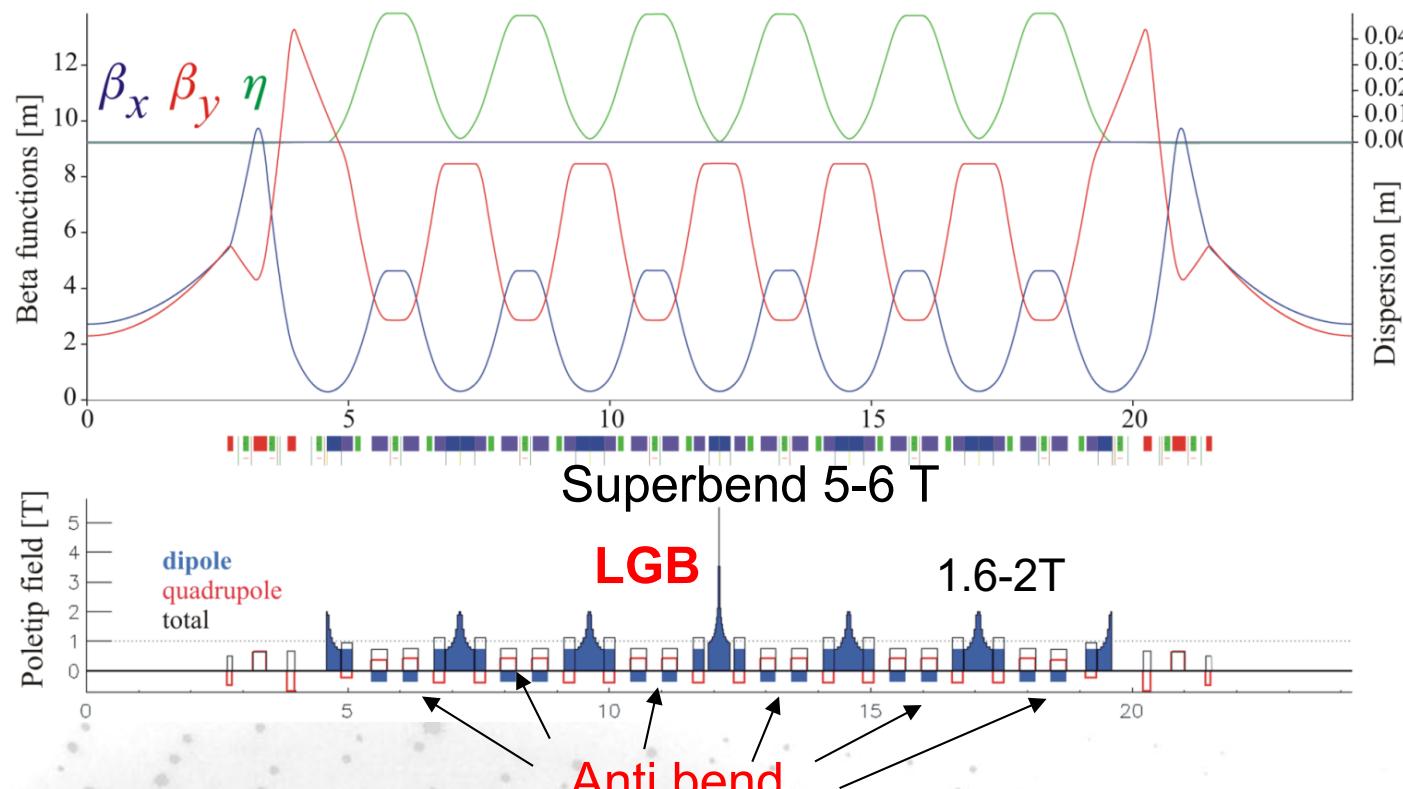
Future:
Introduction of 4 SB of
3.5 T

*12 achromats each made of 6 “cells” invariant to shift between them

SLS-II: LGAB-7BA, 2.4 GeV, 103 pm.rad, N=12, 290 m

Investigation revealed that, due to **low periodicity**, SLS upgrade **could not operate at high chromaticity (-5,-5)**.

Half integer resonance



Symmetry is a MUST

Antibend fully exploited
(585° total absolute angle)

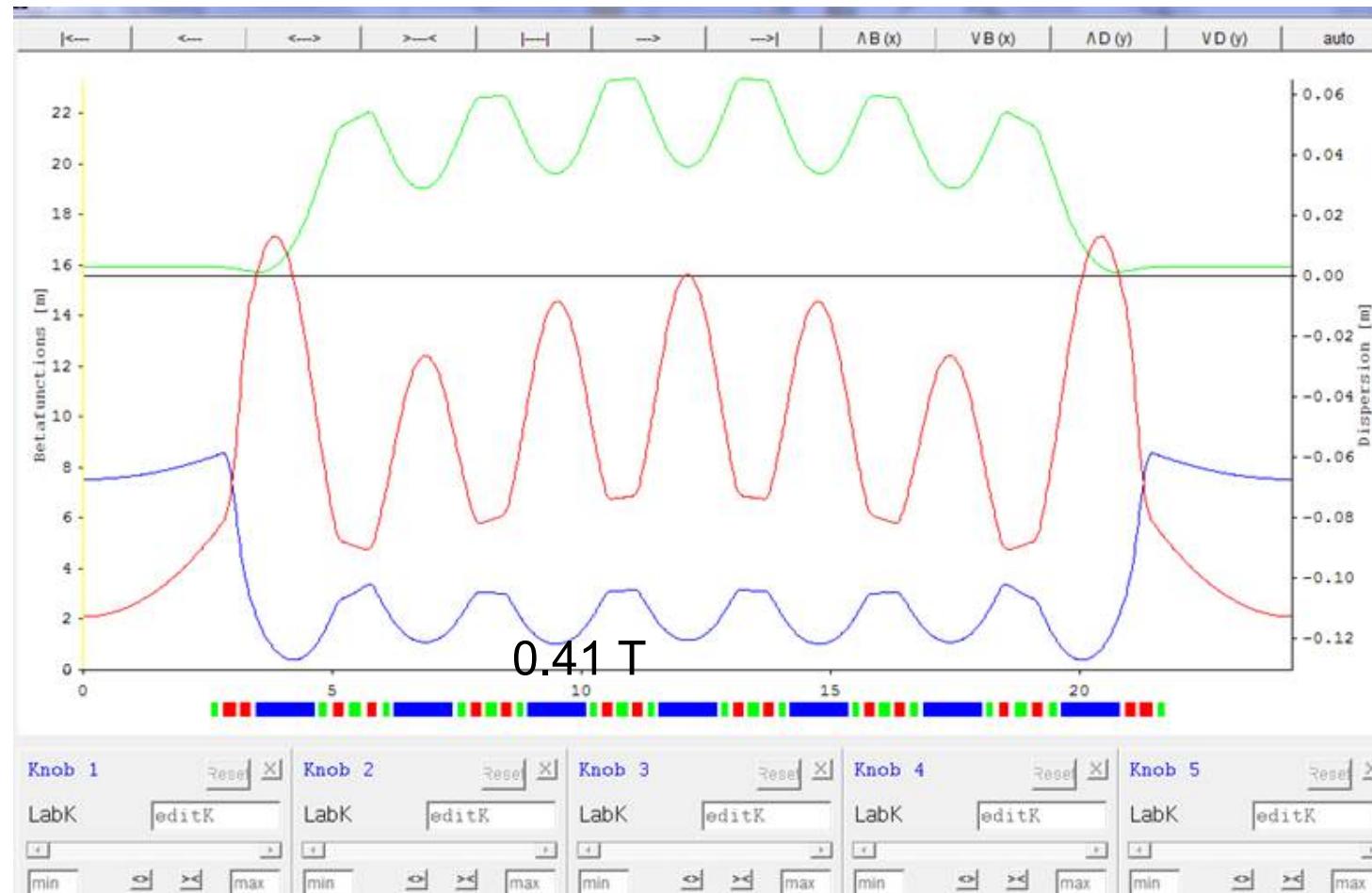
Off-axis injection
Long-axis

⇒ Optical functions

⇒ Magnetic fields
poletip fields for $r = 13$ mm

Low momentum
compaction factor

CLS-II: 7BA, 3 GeV, 186 pm.rad, N=21, 510 m

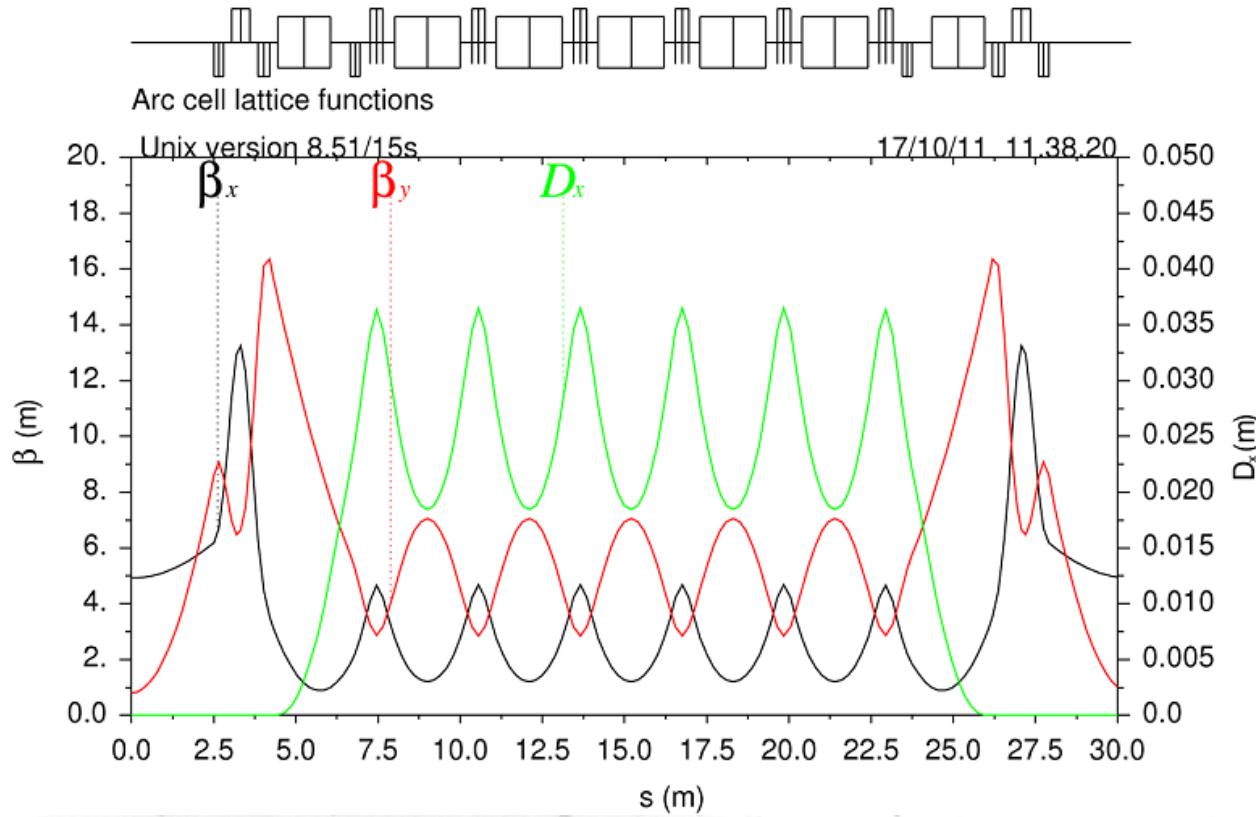


Very preliminary
Results

Off-axis injection

PEPX: 7BA, 4.5 GeV, 11pm, 2199m, 1.5 A

Third and fourth order achromat



$$\mu_x = 4\pi + \pi/4 \quad \text{and} \quad \mu_y = 2\pi + \pi/4$$

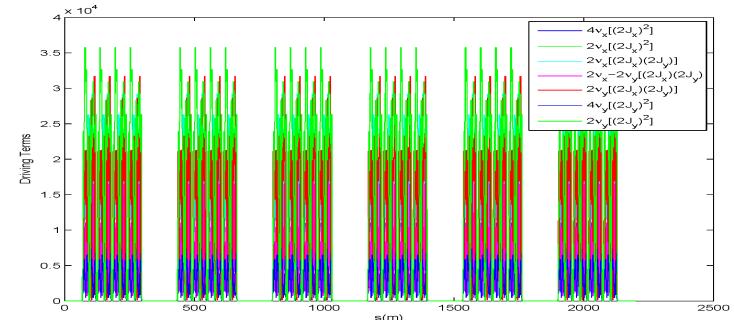
Compact

TME QD replaced with K-dipole

Special phase advance

Sextupole integrated in dipole or quadrupoles

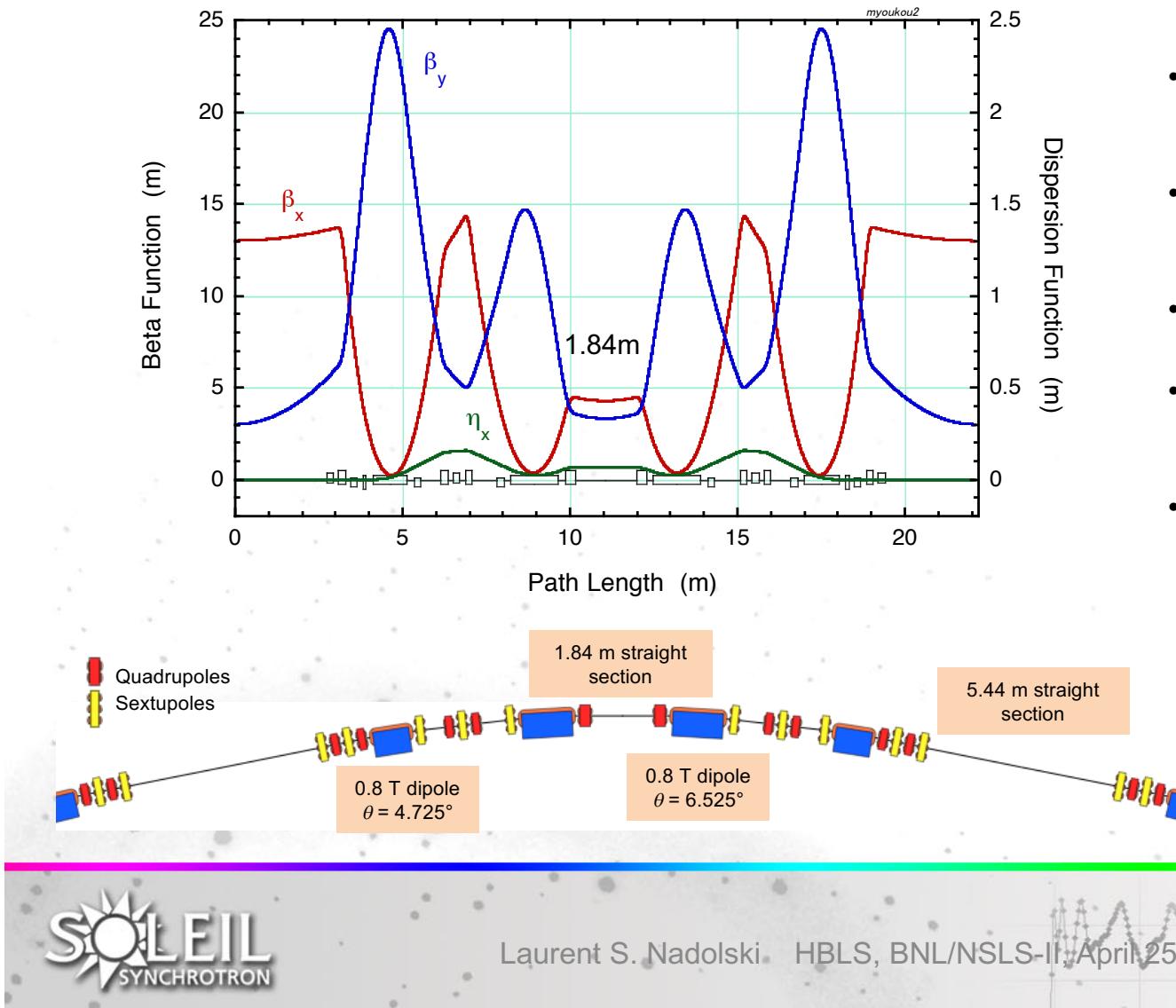
Matching Cell at the end



RDTs

SLiT-J: DDBA, 3 GeV, 920 (720) pm.rad, N=16, 350 m

Synchrotron Light in Tohoku, Japan

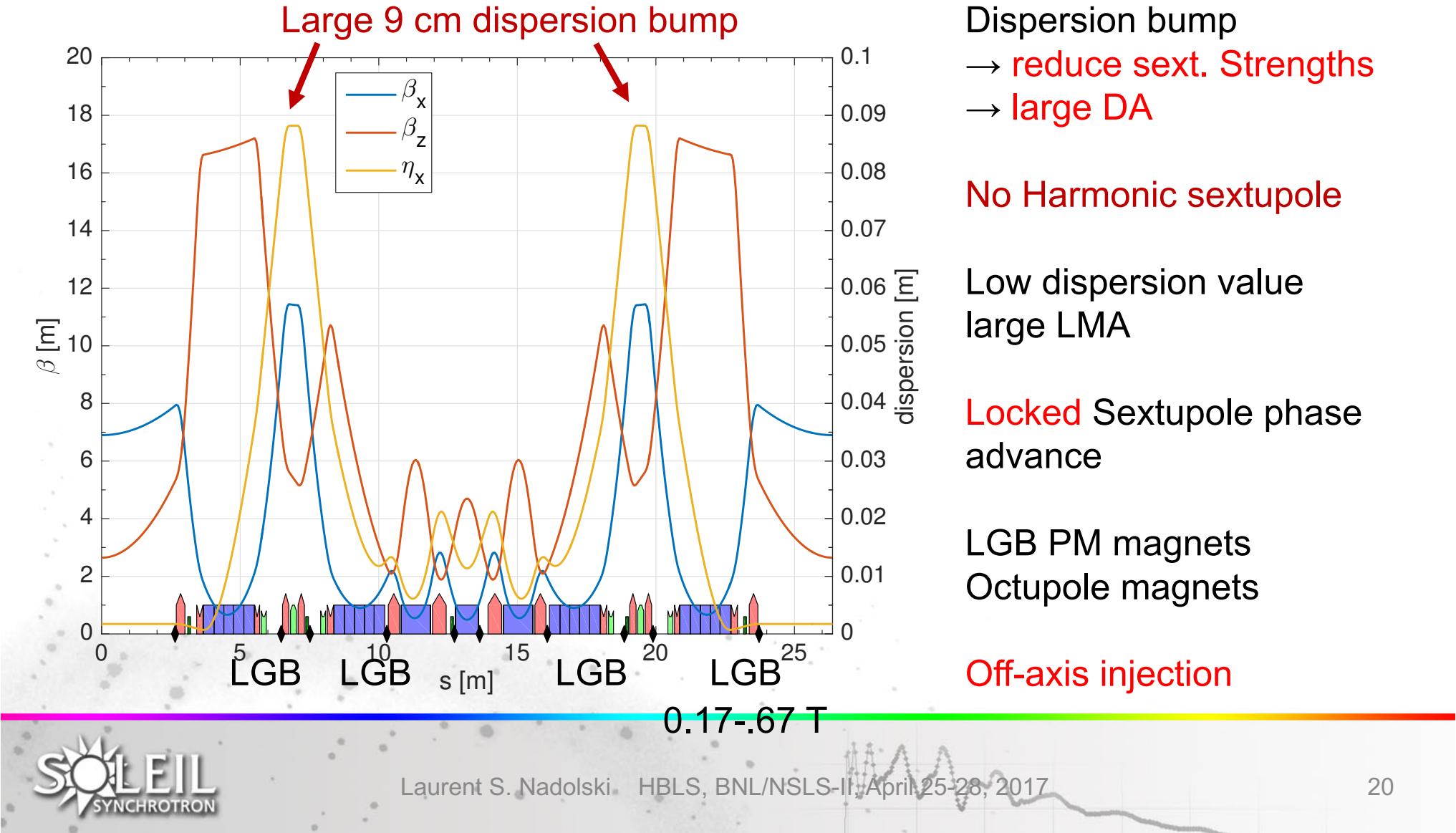


Design a sub-nm emittance storage ring with certain boundary condition ($C \sim 350$ m).

- Start the project as soon as possible (will be approved soon, hopefully).
- Facility size should be compact because of limited available budget.
- Soft X-ray will be **100 times** brighter than that at SPring-8.
- Complete management of saving-energy for high cost-performance facility.
- Secure expansibility and sustainability for the facility.

ESRF-EBS: H7BA, 6 GeV, 135 (110) pm.rad, N=32, 844 m, 200 mA (4b: 40mA, 16b: 80mA)

Collider optics



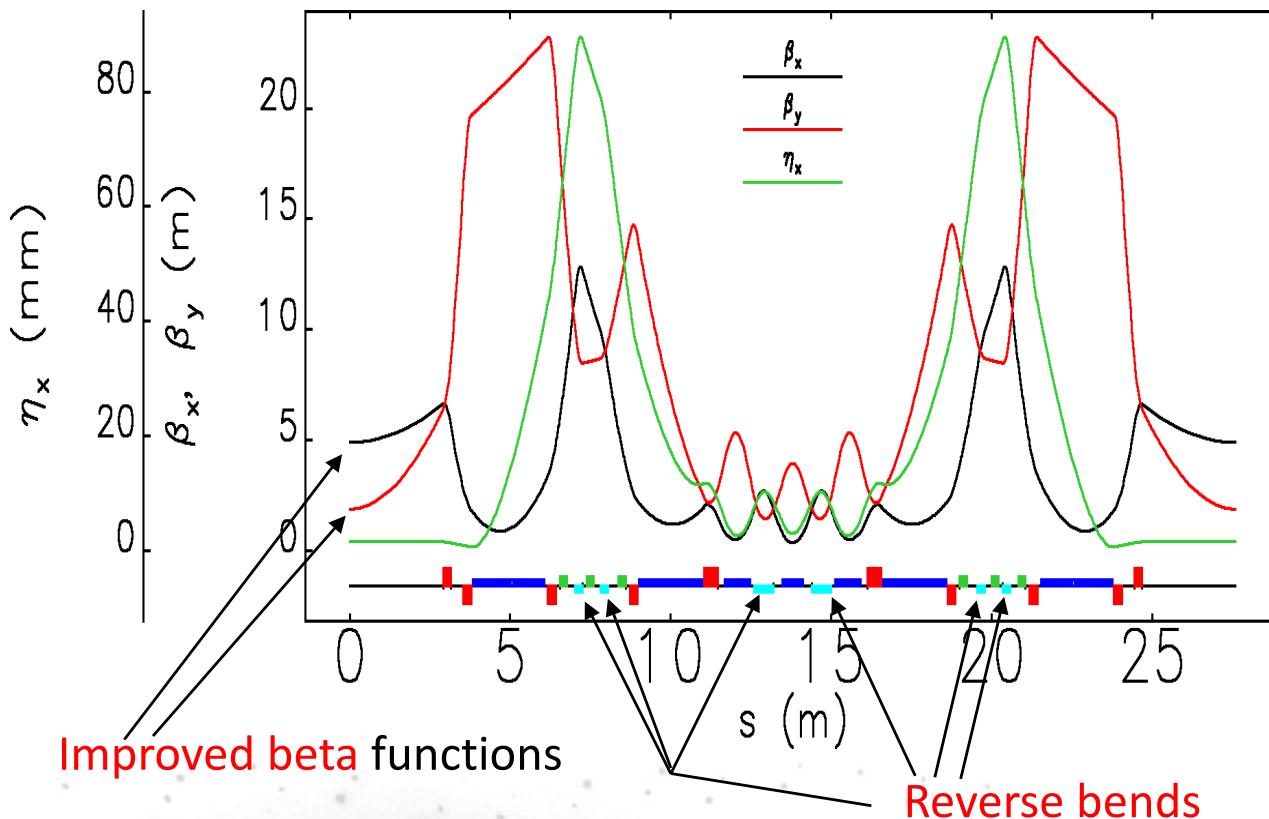
Cell optimization scan

Empirical finding (*) that some observed parameters (knobs) have **effective impact** on physically relevant quantities:

- β_x @ IDs $\rightarrow \varepsilon_x$ (*) P. Raimondi, ESRF
- β_y @ sext $\rightarrow \varepsilon_x, \xi_x$
- α_y @ sext $\rightarrow dQ_y/dA_y$
- K4 @ oct $\rightarrow dQ_x/dA_x$
- φ_y advance between sextupoles $\rightarrow dQ_x/dA_y$

Each parameter scanned individually while keeping others fixed

APS-U: H7BA, 6 GeV, 41 pm.rad, N=40, 1104 m, 200 mA (324b) + time resolved (48b)



- 1: M. Borland et al., NAPAC16, WEPOB01.
- 2: L. Farvacque et al., IPAC13, 79.
- 3: M. Borland et al., IPAC15, 1776.

- 4: J.P.Delahaye et al., PAC89, 1611.
- 5: A. Streun, NIM A 737, 148 (2014).

Start with ESRF-EBS-like H7BA giving 67-pm emittance²

Convert 6 quads/sector to reverse-bends with gradients

- No additional magnets
- Increases energy loss per turn
- Somewhat decouples beta functions and dispersion
- Increases dispersion at the sextupoles

Reduction of sextupole Strength by a factor 3-4

3-pole wiggler (1T)

500 fs FWHM max

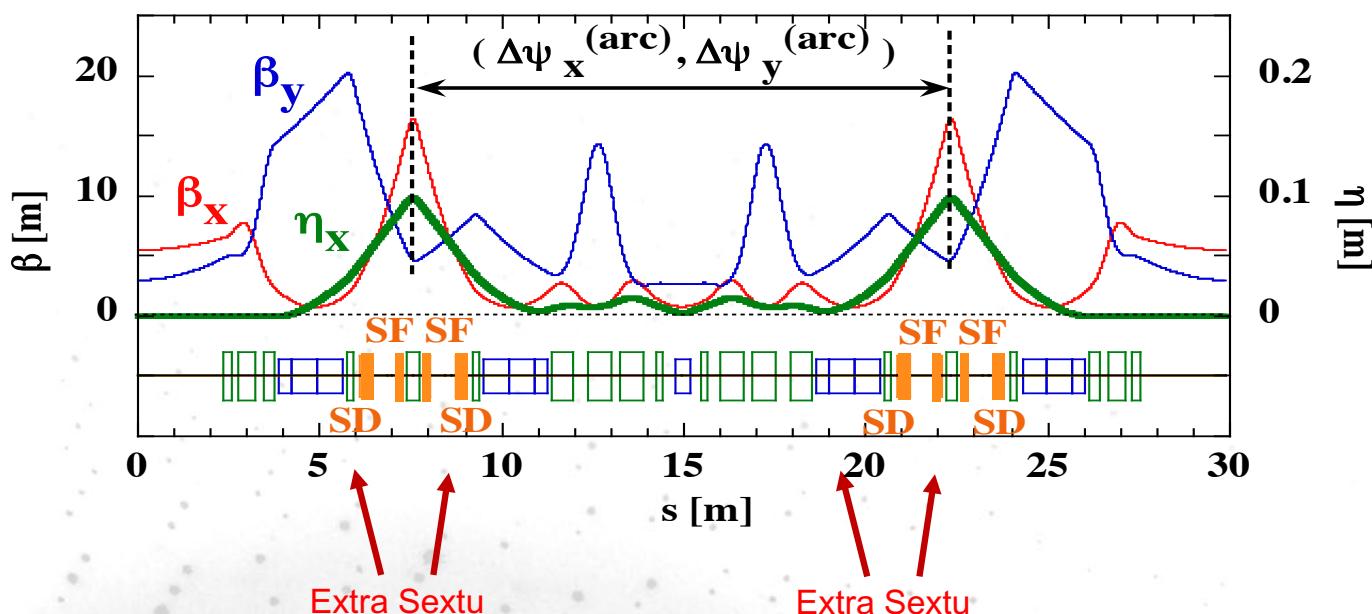
Injection: Swap-out

SPRing8-II: H5BA, 6 GeV, 157 (100) pm.rad, N=40, 1435 m, 100 mA

Practical SR source to allow users to fully use photon performance

1. Chromaticities are compensated by sextupoles at dispersion bumps.
2. Phase advance between bumps is set to $N\pi$ to cancel nonlinear kicks.

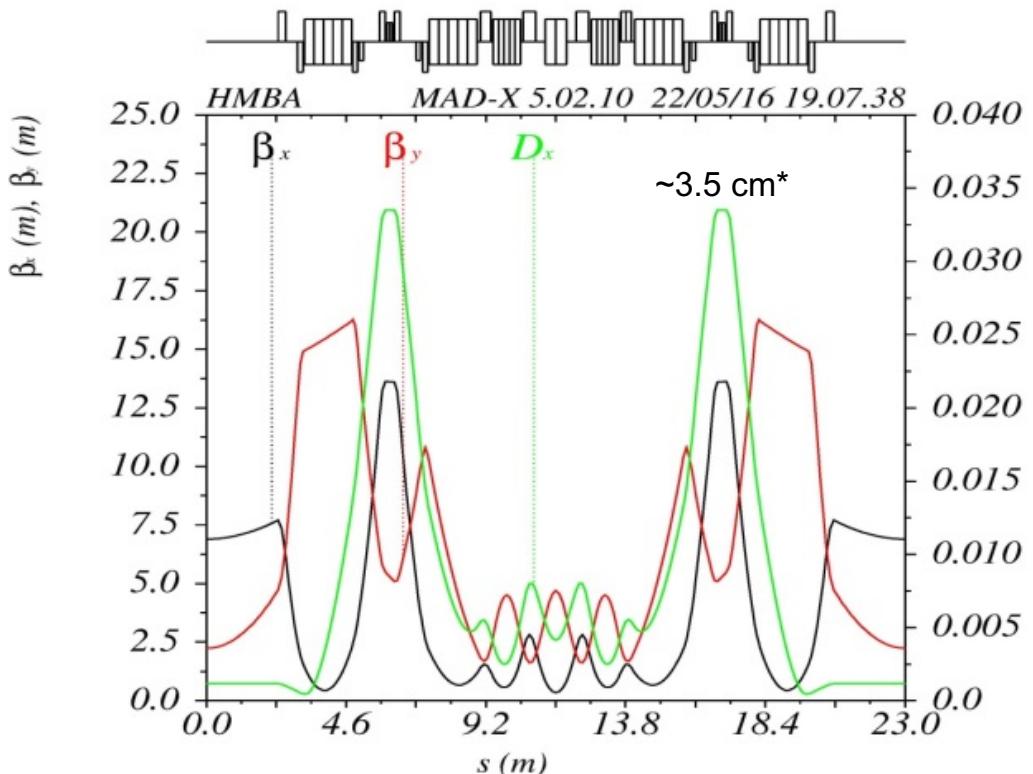
Privilege SACLA for short bunch



Longitudinal Gradient Bend (LGB)

- **Tuning knobs are limited:**
 - A series of sextupoles are closely distributed with each other inside bumps.
 - Phase advance between bumps **should be fixed.**
 - Betatron functions at straight sections should be kept small.
 - Tune at each cell cannot be changed a lot.
- **Injection off (on)-axis**

PETRA-IV: H7BA, 6 GeV, 12 pm.rad, N=72, 2304 m, 200 mA



Lattice based on HMBA Cells

- Arcs: 9 HMBAs cells to build a 45° arc
- 8 identical arcs
- Straight sections: FODO cells

Cell not yet optimized,
(small dynamic aperture) ✗

Dispersion peak: 9 mm → 3.5 mm
Quadrupoles (120 T/m) & sextupoles stronger
→ DA, MA smaller

Try a more relaxed H6BA (or H5BA) cell and include
(vertical) damping wigglers to reduce emittance

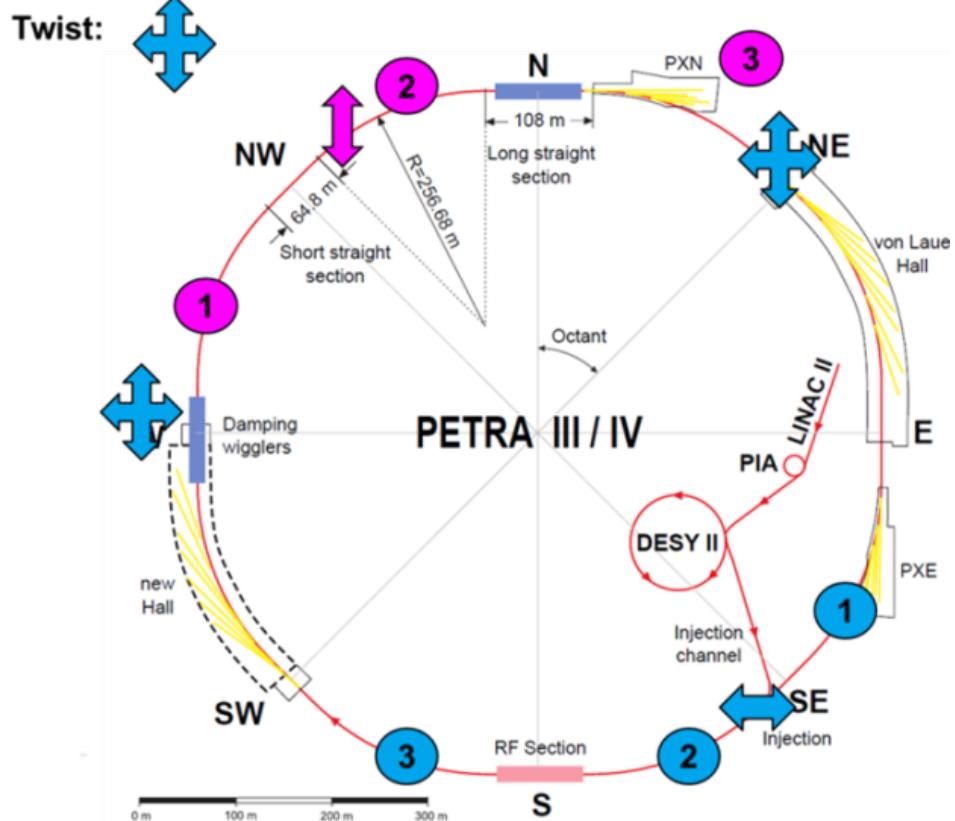
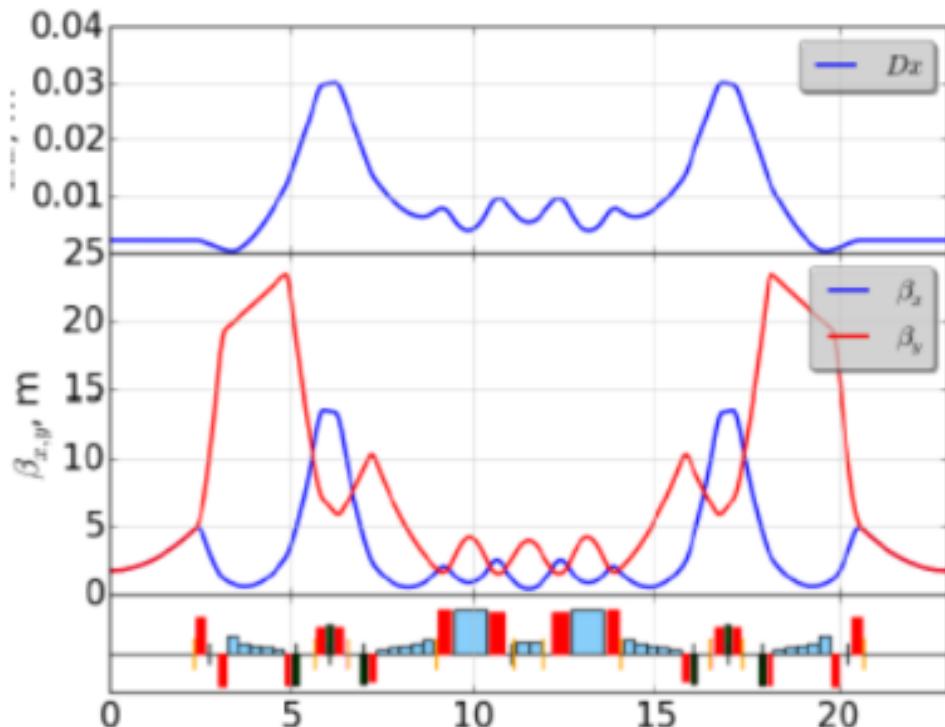
* 9cm for ESRF

FODO cells to connect arcs with matching triplets at both ends
Altogether 4 long (108 m) and 4 short (64.8 m) straight sections



PETRA-IV: H7BA, 5 GeV, 10-30 pm.rad (w/o DW), N=72, 2304 m, 100 mA

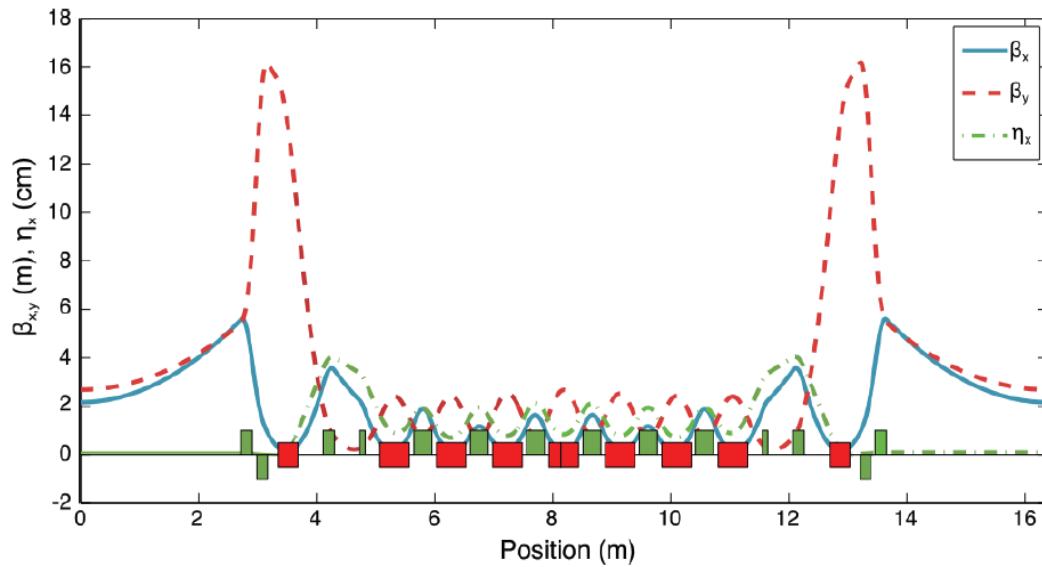
4D-phase space exchange and MBAs



A lattice based on MBAs with
non-interleaved sextupole pairs

Emittance $\sim 20/20$ pm ✓
(5 GeV, wigglers not yet included)
Undulator cell not yet optimized ✗

ALS-U: H9BA, 2 GeV, 109 pm.rad, N=12 (4), 196 m, 500 mA

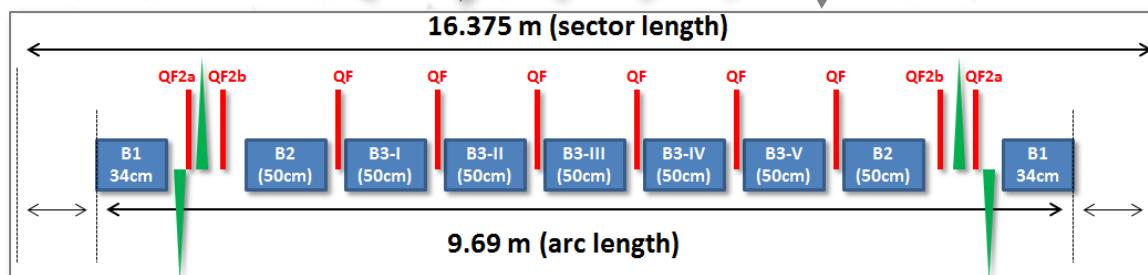


Reversed bending from offset focusing quads

- Symmetric, bare lattice (no IDs, no SuperBends) emittance: $\epsilon_{x0} = 109\text{ pm}$
- w/ full coupling: $\epsilon_x = \epsilon_y = 71\text{ pm}$
- ... including additional damping from ID's: $\epsilon_x = \epsilon_y \sim 55\text{ pm}$
- ... including IBS (with Harmonic Cavities): $\epsilon_x = \epsilon_y \sim 65\text{ pm}$
- Lifetime $\sim 1\text{ hr}$

Super-bend
Injection: Swap-out

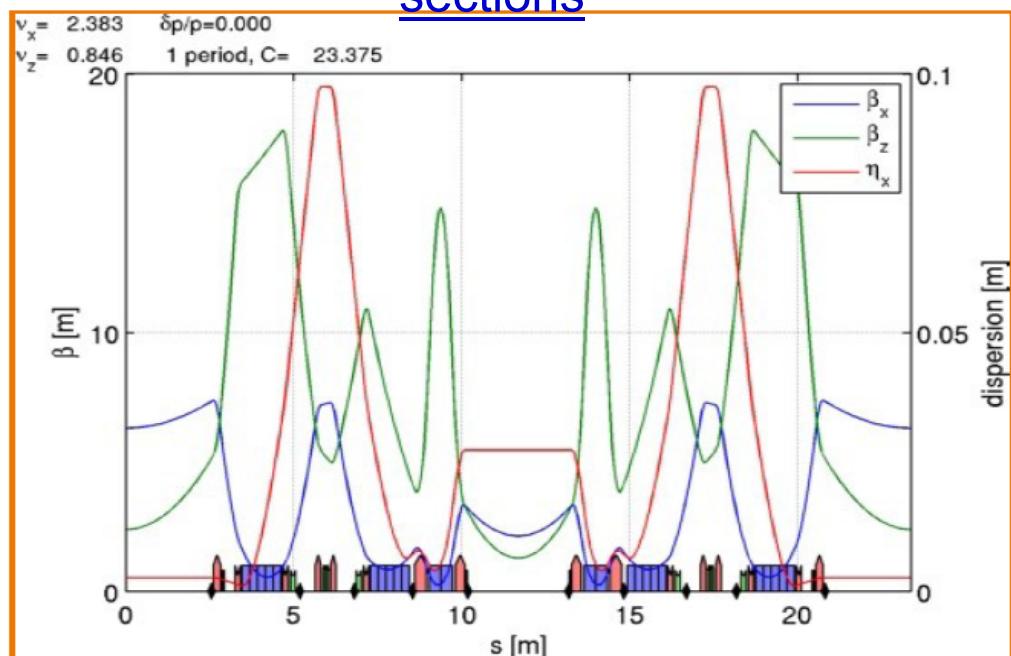
Longer magnet \rightarrow lower field-gradients
 $QF\ K_1 \leq 13.2\text{ m}^{-2}$ (88 T/m)
 Central bend $|K_1| \leq 6.3\text{ m}^{-2}$ (42 T/m)
 Similar magnet designs as for the 9BA lattice



DIAMOND-II: DTBA/M6BA, 3 GeV, 100-140 pm.rad, N=24, 561 m

Diamond II design is striving to combine

low emittance **and** doubling the straight sections



Use the ESRF cell concept (7BA with longitudinal gradient dipoles) –
removing the mid dipole to make it a 6BA with a straight at the centre

Longitudinal gradient
dipoles + strong gradient
dipole (up to 1.4 T 40 T/m)

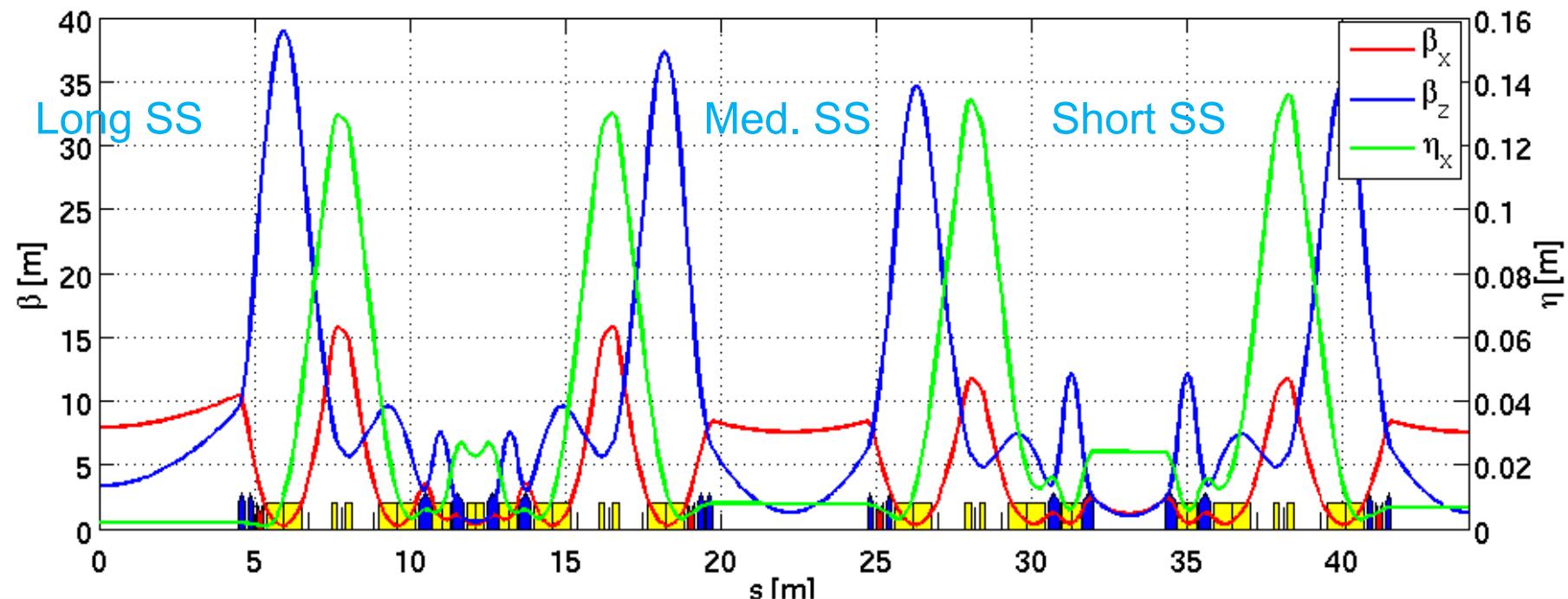
~3 m mid-straight section

Off-axis injection

SS 8.0/5.2/3.0

Collaborative work DIAMOND/ESRF

SOLEIL-II: H6BA-H7BA, 2.75 GeV, 190-230 pm.rad, N=4 (16), 354.1 m



Very Compact lattice



Standard lattice do not apply: 24 straight sections

Off-axis injection

Straight Section length : 9 m, 5 m and 2.8 m Straight / Circumference ~ 32 % (45% today)

Main magnets : Bend : 0.6 T and 30 T/m No LGB, **Use of reverse-bend in dispersion bump**
Quad : 70 T/m max, Low Sext value : 700T/m²

Conclusions

	Energy	circumference	emittance	emit/gamma^2	Lattice	Qx	Qy	Q'x	Q'y	Optics strain**	Cell length	Cell #
PETRA-IV	6	2304	10	7,3E-08	H7BA							NA
Pep-X	4,5	2200	30	3,9E-07	7BA	113,23	65,4	-162	-130	2,8	30	NA
Spring8-II	6	1436	67	4,9E-07	H5BA	108,1	45,6	-143	-147	4,3	30	40
APS-U	6	1104	41	3,0E-07	H7BA	95,1	36,1	-131	-122	4,7	27,6	40
ESRF-EBS	6	844,4	133	9,6E-07	H7BA	76,21	27,34	-109	-82	4,3	26,4	32
DIAMOND-II	3	561	120	3,5E-06	DTBA	58,18	21,31	-77	-118	7,3	22,6*	24
MAX-IV	3	528	328	9,5E-06	7BA	42,2	16,28	-50	-50	3,6	26	20
SIRIUS	3	518	240	7,0E-06	5BA	49,11	14,17	-119	-81	13,9	25,9	20
CLS-II	3	510	186	5,4E-06	7BA	37,22	10,32	-66,7	-40,4	7,0	24,3	21
SOLEIL-II	2,75	354,1	200	6,9E-06	H6BA-H7BA	39,12	14,24	-75	-85	11,4	22*	16
SLIT-J	3	350	600	1,7E-05	DDBA	29,21	9,28	-69,3	-41	10,5	21,9	16
SLS-II	2,4	290	100	4,5E-06	7BA	37,22	10,32	-66,6	-40,4	7,0	24,1	12
Elettra-II	2	259,2	250	1,6E-05	S6BA	33,2	9,3	-63	-50	10,2	12,6	12
ALS-U	2	196,8	109	7,1E-06	9BA	41,38	20,39	-64	-67	5,1	16,35	12

****Optics strain = $Qx'/Qx \cdot Qy'/Qy$**

Compact & Rigid lattice Exotic magnets

TGB / LGB

Combined function - magnets

Hybrid MBA more adapted for large storage ring (sextupole strength relaxed)

Relevant cell length is the one limited to magnetic structure

Anti-bend relaxes fairly nicely the constraints on the emittance and increases tunability

High periodicity is privileged for ultra-low emittance lattices

**3-4 % LMA
Low MCF**

Thank You for Your Attention

Acknowledgement

- R. Nagaoka, A. Loulergue, P. Brunelle, A. Nadji, H.-C. Chao, M.-A. Tordeux (SOLEIL)
- A. Streun (SLS), E. Karanzoulis (Elettra), R. Bartolini (DIAMOND), L. LIN (SIRIUS), L. Farvacque (ESRF), P. Tavarez (MAX-IV), R. (PETRA-IV), M. Borland (APS-U), Q. Qin (HEPS), H. Hama (SLiT-J), H. Tanaka and K. Soutome (SPRing8-II), L. Dallin (CLS), C. Steier (ALS-U)